

**Sebastian Król**

*Adam Mickiewicz University Poznań, Poland*

## The maximal regularity estimates for abstract evolution equations

It is a well-known fact that the solvability of the abstract inhomogeneous Cauchy problem

$$u' + Au = f \quad \text{with} \quad u(0) = x \in X \quad (\text{ACP})$$

depends essentially on the geometry of the underlying Banach space  $X$ . In this context, the classical results due to Da Prato and Grisvard assert that such solvability improves significantly if (ACP) is considered in the real interpolation spaces between  $X$  and the domain of  $A$ . After a brief discussion of this phenomenon, I will present an extension of Da Prato-Grisvard theory that has new and noteworthy implications for the solvability of (ACP).

### References.

- [1] S. Król, M. Mastyło, J. Sarnowski, *Maximal regularity estimates for the abstract Cauchy problems*, preprint
- [2] S. Król, J. Sarnowski, *The invariant subspaces of periodic Fourier multipliers with application to abstract evolution equations*, arXiv:2301.12451
- [3] S. Król, *The maximal regularity property of abstract integro-differential equations*, J. Evol. Equ. 23 (2023)